Predicting Radionuclide Release Rates from Spent Nuclear Fuel Inside a Failed Waste Disposal Container Using a Finite Element Model

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Models for the corrosion of spent nuclear fuel (fission and actinide-doped uranium dioxide) provide the essential source term for the release of radionuclides from within a failed nuclear waste container in a deep geologic repository. Although redox conditions within a repository are expected to be anoxic, exposure of the fuel to groundwater will cause the generation of oxidants at the fuel surface, leading to its corrosion and the release of radionuclides. The influence of these oxidants will be partially mitigated by the anoxic corrosion of the inner walls of the steel container to produce the oxidant scavengers, Fe$^{2+}$ and H$_2$. This review summarizes the development of a finite element model developed to determine the influence of the various redox-controlling species (H$_2$O$_2$, Fe$^{2+}$, H$_2$). Both one-dimensional and two-dimensional models are described, with the latter required to take into account the fractured geometry of the fuel.

KEY WORDS: COMSOL, corrosion, modeling, spent nuclear fuel, uranium dioxide, waste disposal

INTRODUCTION

The universally accepted approach for the safe disposal of spent nuclear fuel is to bury it in a deep geologic repository (DGR). The accepted repository concept is based on multiple barriers, including the fuel waste form, durable metal containers, a clay buffer and seals around the container, and the stable geologic formation, Figure 1. The corrosion resistant container is expected to be a key barrier in this sequence, isolating the fuel from the repository environment. In Canada, Sweden, and Finland, the proposed container comprises a steel vessel, or insert, with an outer barrier layer of copper, in the form of either a shell or a deposited coating.1

While there is confidence that long-term containment can be achieved, it is judicious to examine the possible consequences of container failure, which could allow contact of the fuel with groundwater. Although anoxic conditions are expected to prevail in a DGR, the radiation fields associated with the fuel waste form could lead to the generation of oxidants by groundwater radiolysis within a failed container. Radiolytically-produced H$_2$O$_2$ is expected to be the dominant oxidant,2 which can oxidize the insoluble U$^{IV}$ in the UO$_2$ fuel to the more soluble U$^{VI}$ (as UO$_2$$^2-$), leading to the corrosion of the fuel and the release of radionuclides to the groundwater.2-3

Within the failed container, there will be two corrosion fronts: one on the fuel surface driven by the radiolytic oxidants, and a second on the inner surface of the carbon steel vessel or Fe insert, driven by the reduction of H$_2$O. The redox condition within the container will be inevitably influenced by the soluble Fe$^{2+}$ and H$_2$, produced by the second corrosion process,4-6 Figure 2. As illustrated in the figure, the redox coupling of the two corrosion fronts could potentially lead to the scavenging of the radiolytic oxidants and a suppression of the fuel corrosion/radionuclide release processes.

A considerable experimental effort to acquire the databases required to develop models to predict the fuel corrosion process has been undergone, and reviews have been published.7-8 Of these models, three have attempted to account for the influence of fuel corrosion of the evolution of redox conditions with time inside a failed container.9-11 Two of the three models9-10 are one-dimensional electrochemical reaction/diffusion models based on mixed potential theory, which enables them to predict the evolution of the fuel corrosion potential and corrosion current as the radiation fields within the fuel decay with time. The third model is a chemical reaction/diffusion model originally developed in one-dimensional (1D) form,11 but recently extended to two-dimensional (2D) form.12 The 2D model takes into account the complex geometry of spent fuel, in particular, the extensive fracturing that occurs due to the stress from thermal tension during in-reactor irradiation and during the cooling that occurs on removal of the fuel from the reactor.13 These fractures provide primary pathways for groundwater access to deep locations within the fuel, where the scavenging of radiolytic oxidants by the products of steel corrosion could be limited.
This review summarizes the progress made on the development of this last model. The emphasis is placed on evaluating how the various processes possible within a failed container will influence the redox conditions at the fuel surface, and hence, the corrosion behavior of the fuel.

MODEL DESCRIPTION

2.1 | Essential Spent Fuel Properties

The universally common form of nuclear fuel is stoichiometric UO₂, fabricated as high density (94% to 97% of theoretical) ceramic pellets and contained within Zircaloy sheathing. The basic chemical and physical properties of UO₂ have been summarized.\(^\text{14}\) While the solubility of UO₂ is extremely limited,\(^\text{15}\) it increases substantially under oxidizing conditions, making the stability of fuel strongly dependent on the redox conditions to which it is exposed.

The chemical changes to the fuel induced by in-reactor irradiation have been described elsewhere.\(^\text{16}\) The fuel can be considered to be a rare-earth (RE\(^{\text{III}}\))-doped UO₂ matrix containing segregated noble metal (ɛ) particles.\(^\text{16}\) Both the extent of RE\(^{\text{III}}\)-doping and the number density of ɛ-particles increase with the extent of fuel burn-up, leading to the improvement of the electrical conductivity of the fuel matrix. From the corrosion perspective, the fuel can be considered a conductive/reactive matrix containing noble metal (Pd, Ru, Rh, Mo) particles, which can act as either anodes or cathodes, depending on the prevailing redox conditions.

2.2 | Model Reactions

Figure 3 shows the main reactions involved in controlling the redox conditions, and hence, the process of fuel corrosion. This reaction scheme has been established based on extensive international experimental programs. The model includes the following reactions:

(i) The production of H₂O₂ and H₂ by H₂O radiolysis (1).

(ii) The corrosion of UO₂ supported by the reduction of H₂O₂ on the UO₂ surface (2a) and on ɛ-particles (2b).

(iii) The reduction of oxidized surface species (UV and UVI) by H₂ oxidation on ɛ-particles (3a); of dissolved UO₂\(^{3+}\) by H₂ in solution (3b); and of adsorbed UO₂\(^{3+}\) by H₂ activated on ɛ-particles (3c).

(iv) The consumption of H₂O₂ by reaction with soluble Fe\(^{2+}\) (4).

(v) Surface reaction between H₂O₂ and H₂, catalyzed by ɛ-particles (5).

(vi) The decomposition of H₂O₂ to O₂ and H₂O at the UO₂\(±x\) surface (6).

The kinetics of these reactions have been discussed in detail elsewhere.\(^\text{12,16}\) It is assumed that groundwater contains a sufficient HCO₃⁻/CO₃\(^{2-}\) to completely complex and dissolve the corrosion products in the form of UO₂(HCO₃)\(^{2-}\); as a result, no corrosion products would deposit on the surface to impede the dissolution of the waste form as UO₂\(^{4+}\). The rates of the various reactions are described by a series of 1D reaction-diffusion equations. The mathematical model is numerically solved using COMSOL Multiphysics\(^\text{11}\), based on the finite element method using the chemical engineering and dilute species transport modules. The values of the parameters used in calculations have been listed and discussed in detail elsewhere.\(^\text{11,12,17}\)

2.3 | Radiolysis Model

Only α-radiolysis is considered as a source of oxidants, as it is reasonable to assume that containment will be maintained for the few hundred years required for γ/β radiation fields to decay to innocuous levels. Figure 4.\(^\text{16}\) The dose rate is non-uniformly distributed along the very short penetration pathway of α-particles. Despite this feature, the model assumes a uniform distribution within a radiation zone of 13 μm at the fuel/H₂O interface, as illustrated in Figure 5.\(^\text{19}\) The basis for the adoption of such a layer has been discussed previously.\(^\text{11}\) The consequences of this assumption have been analyzed\(^\text{11}\) and shown to have only a marginal effect on model calculations.

Only the molecular species, H₂O₂ and H₂, are used in calculations, despite radiolysis measurements and models demonstrating the formation of a wide spectrum of radical species. This approximation is justified because the steady-state concentrations of radicals generated by continuous α-radiolysis are 2 to 5 orders of magnitude lower than those of the stable molecular products. Compared to the model calculations based on a full set of α-radiolysis reactions (i.e., including

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\(^1\) Trade name.
those involving radical production), the calculations based on the simplified model (only including H₂O₂ and H₂ production) show an overestimate of [H₂O₂] by 21% and of [H₂] by ∼3%.

The reasons for the overestimation of [H₂O₂] could be: (1) the modification of the G-value for H₂O₂ from 0.104 μmol/J to 0.1248 μmol/J; or (2) the radicals produced will effectively recombine to yield H₂O₂ (2OH → H₂O₂; H + HO₂ → H₂O₂). This overestimation leads to an increased [UO₂²⁺] by a conservative 20%. Model calculations are performed using an average α dose rate at the fuel surface of 9.03 × 10⁵ Gy a⁻¹, calculated for a typical CANDU fuel bundle with a burn-up of 220 MWh/kgU at 1,000 y after discharge from reactor.

ONE-DIMENSIONAL (1D) AND TWO-DIMENSIONAL (2D) MODELS

3.1 | One-Dimensional (1D) Model

Figure 6 shows the characteristics of the fuel/groundwater interface, with x indicating the distance from the fuel surface, and b the thickness of the uniform radiation zone. The diffusion layer is the distance over which species can diffuse to, and from, the fuel surface, and beyond which uniform concentrations of all species are presumed to prevail. The length of this layer can be taken to represent the distance of the spent fuel surface from a flaw in the cladding, beyond which the concentrations of Fe²⁺ and H₂ ([H₂]bulk) generated by carbon steel corrosion are constant (i.e., a constant corrosion rate of the steel is assumed) and the concentrations of species produced at the fuel surface (i.e., H₂O₂ and UO₂²⁺) reach zero. This allows the [Fe²⁺] and [H₂] adopted to represent different steel corrosion rates without the need to incorporate a specific corrosion model.

The efficacy and validity of adopting such an approach has been evaluated. Model sensitivity calculations showed that varying the diffusion length over 3 orders of magnitude caused only a change in fuel corrosion rate of a factor of 2. In addition, a combined experimental/modeling study was undertaken to investigate the possibility of passivation of the steel surface inside a failed waste container. In the experimental part, the corrosion of carbon steel was studied by adding small amounts of 

\[ \text{H}_2 \text{O}_2, \text{H}_2, \text{etc.} \]

\[ \text{Fe}^{2+}, \text{UO}_2^{2+} \]

\[ \text{OH}^- \]

\[ \text{Fe}^{3+} \]

\[ \text{O}_2, \text{H}_2 \text{O} \]

\[ \text{U}^{IV} \]

\[ \text{U}^{VI} \]

\[ \alpha \]

\[ \beta \]

\[ \gamma \]

\[ \epsilon \]

\[ \delta \]

\[ \zeta \]

\[ \eta \]

\[ \chi \]

\[ \theta \]

\[ \vartheta \]

\[ \kappa \]

\[ \lambda \]

\[ \mu \]

\[ \nu \]

\[ \xi \]

\[ \omicron \]

\[ \pi \]

\[ \rho \]

\[ \sigma \]

\[ \tau \]

\[ \upsilon \]

\[ \phi \]

\[ \chi \]

\[ \psi \]

\[ \omega \]
concentrations of H$_2$O$_2$. By adapting a previously developed 1D model$^{12}$ for fuel and steel corrosion, calculations were performed to simulate the [H$_2$O$_2$] expected on the inside surface of the steel. The adapted model takes account of the long-term corrosion rate of steel under anaerobic conditions (around 0.1 μm/y). This study demonstrated that radiolytically-produced oxidants (i.e., H$_2$O$_2$) could not achieve sufficiently high concentrations at the steel surface to induce passivation, thereby suppressing the steel corrosion rate and inhibiting the supply of the radiolytic scavengers, Fe$^{2+}$ and H$_2$.

3.2 | Two-Dimensional (2D) Model

As spent fuel is heavily fractured and possesses a large number of fission gas bubbles/tunnels, especially along grain boundaries, there is the possibility that the groundwater will penetrate deep within the fuel, leading to the local accumulation of radiolytic species at locations inaccessible to the oxidant scavengers from steel corrosion. To investigate the potential consequences of such physical features, the model was extended to 2D. The 2D arrangement adopted is illustrated in Figure 7. A simplified rectangular geometry is adopted for the cross-sectional area and the dimensions of a fracture determined by its width and depth. α-particle emission is assumed to occur uniformly across the surface, which can be considered wrapped in a thin radiation zone. The diffusion zone, defined above, is retained. In this geometric arrangement, the dose rate is uniformly distributed except at the deep corners of the fracture, where it will be doubled, and at the top of the fracture, where it will be reduced.

THE INFLUENCE OF VARIOUS CHEMICAL AND PHYSICAL FEATURES ON FUEL CORROSION RATES

4.1 | The Influence of Fe$^{2+}$

The Fe$^{2+}$ ions produced by the anoxic corrosion of steel will undergo the Fenton reaction (Figure 3, Reaction [4]). This reaction is considered irreversible for the pH range anticipated in groundwater (6 ≤ pH ≤ 9), because the solubility of Fe$^{3+}$ will be <10$^{-38}$ mol/L and 2 to 4 orders of magnitude lower than that of Fe$^{2+}$. To account for possible variations in the corrosion rate of the steel, the [Fe$^{2+}$] was varied over the range 0.01 μmol/L to 1 μmol/L and its influence on H$_2$O$_2$ consumption and, hence, the fuel corrosion rate calculated. Figure 8 shows the influence of [Fe$^{2+}$] on the [H$_2$O$_2$] profile at the fuel/solution interface calculated using the 1D model.

![Figure 6. Illustration of the 1D α-radiolysis model.](image)

![Figure 7. Model arrangement showing a cross section of the fuel/solution interface for the simulation of radiolytic corrosion inside a fracture in a fuel pellet. The area in blue indicates the diffusion zone, and the region at the fuel surface within the dashed red line indicates the radiation zone.](image)

![Figure 8. The influence of Fe$^{2+}$ (from steel corrosion) on the [H$_2$O$_2$] profile at the fuel/solution interface calculated using the 1D model.](image)
4.2 | The Influence of H2

A considerable effort has been expended on the study of the effect of H2 because it appears to have the potential to completely suppress fuel corrosion.22-23 Calculations indicate that dissolved [H2] as high as ∼40 mmol/L could be generated as a consequence of steel corrosion in sealed repositories. The key requirement for H2 to suppress fuel corrosion is that a mechanism be available to activate H2 by dissociation to produce H+ radicals on the fuel surface. A range of studies have shown that this can be achieved by catalysis on α-particles23 and by interaction of solutions containing H2 with either γ or α radiation,22-23 with the latter path involving the reaction of OH+ (an H2O radiolysis product) and H2 to produce H+ radicals (Wu, et al.,17 and references therein).

As shown in Figure 3, there are a number of pathways by which H2 can influence fuel corrosion. The mechanistic and kinetic details of these reactions have been discussed in detail elsewhere.22-26 Besides production by steel corrosion, H2 will also be generated radiolytically. Calculations using the 1D model showed the influence of radiolytic H2 production appeared to be minor compared to that produced by steel corrosion. This was demonstrated by sensitivity calculations performed with and without the contribution of radiolytic H2 in the presence of relatively small [H2] from steel corrosion (0.01 μmol/L). Ignoring radiolytic H2 leads to an increase in the fuel corrosion rate by ∼10%.

As Fe2+ can also suppress the corrosion rate (discussed above), the amount of H2 required to completely suppress fuel corrosion (defined as the critical H2 concentration, [H2]crit) was calculated with a specified [Fe2+]i. Figure 9 shows the required [H2]bulk in the absence of Fe2+ as well as over the range of [Fe2+]i considered above, and demonstrates that, even if the ability of Fe2+ to scavenge H2O2 is not considered, an [H2]crit of only ∼0.2 μmol/L is required to completely suppress fuel corrosion. This represents a miniscule requirement when compared to the ∼40 mmol/L potentially available in a sealed DGR.22

Within fractures in the fuel, it is possible radiolysis could lead to the accumulation of radiolytic oxidants inaccessible to externally produced reductants, which was investigated using the 2D model. Calculations show that, as the depth of fractures increases, the [H2] increases significantly while the [H2O2] reaches a plateau. Considering that the primary radiolytic yields are the same for the two species in the model, this difference can be attributed to a number of features: (i) the externally supplied H2; (ii) H2 is stable whereas H2O2 is consumed by its decomposition to yield the much less reactive O2;27-28 and (iii) H2O2 and H2 react with the fuel surface at different rates.17 This imbalance between [H2O2] and [H2] influences the competition between UO2 oxidation by H2O2 and its reduction by H2.

In the 2D simulation, the corrosion rate of spent fuel (represented by the diffusive flux of UO22+ in the direction normal to the surface, Figure 10), reaches a maximum near the mouth of the fracture, and approaches zero at the base of the fracture, the latter indicating a very significant suppression of corrosion. As the access of external reductants, Fe2+ and bulk H2, to deep locations within the fracture is limited, this suppression reflects the accumulation of radiolytic H2, which is greatest at the base of the fracture.

The variation in corrosion rate along the fracture walls can be attributed to the variations in [H2O2] and [H2]; the former remaining constant while the latter increases with depth. As the fracture mouth is approached, the rapid decrease in corrosion rate is attributed to the prompt decrease in [H2O2], as it (1) diffuses out of the fracture; and (2) is consumed by the Fe2+ diffusing in. By separating the contributions to corrosion suppression by internal (radiolytic) and external (steel corrosion) H2, the role of the former at deep locations was confirmed.29 To obtain the [H2]crit, the UO22+ flux in the direction normal to the fuel surface (equivalent to the corrosion rate) was calculated as a function of [H2]bulk. The [H2]crit is taken to be achieved when corrosion is completely suppressed at all surface locations. To simulate the range of fracture geometries anticipated in fractured fuel pellets, [H2]crit was calculated for a wide range of fracture depths and widths. Figure 11 shows [H2]crit increases to a peak value and then decreases as the fracture deepens. Within the fracture dimensions tested, [H2]crit never exceeds a maximum contribution from external (bulk) H2 of 2.4 μmol/L, indicated by the dashed line in Figure 11. This value is ∼12 times the [H2]crit required to completely suppress corrosion on a planar surface, demonstrating that, while a larger contribution of H2 from steel corrosion is required in fractures, the demand is not high.
CANNOT BE CONSIDERED TO
STRENGTH WAS ESTABLISHED. IN FIGURE 13, THREE SETS OF DATA
LED TO UNEXPECTEDLY LOW VALUES. THE VALUES LABELED C WERE
MEASURED IN A CLAY ENVIRONMENT CONTAINING REDUCING SPECIES,
LED TO THE OVERESTIMATION OF THE RATES. THE VALUE LABELED B WAS
WHICH LARGE ERRORS DUE TO THE HIGH RESISTANCE OF THE MATERIALS
ELECTROCHEMICAL IMPEDANCE SPECTROSCOPY MEASUREMENTS, IN
THAT OXIDATION (TO O2 AND H2O) HAS YET BEEN DEVELOPED, H2O2
DECOMPOSITION, THE INCREASE AS THE FRACTURE DEPTH INCREASES, BUT INCREASES AS THE FRACTURE DEPTH INCREASES. AS O2, AN ALTERNATIVE OXIDANT FOR UO2, IS PRODUCED BY DECOMPOSITION, THE INFLUENCE OF THIS REACTION REMAINS TO BE FULLY INVESTIGATED.

**4.3 | The Influence of H2O2 Decomposition**

While no complete kinetic understanding of H2O2 decomposition (to O2 and H2O) has yet been developed, H2O2 decomposition will influence the demand for [H2]bulk to suppress corrosion, although the influence is not expected to be major. Experimental and theoretical calculations on UO2 and a range of transition metal oxide surfaces show that decomposition proceeds via the formation of OH+ radicals. By comparing the amount of H2O2 consumed to the amount of U dissolved, it was shown that H2O2 decomposition was the major pathway for its consumption, with the dissolution yield for simulated high-burn-up UO2 fuel (SIMFUEL) being considerably less (0.2%) than that for pure UO2 (14%). Recent electrochemical results demonstrate that this can be attributed to stabilization of the UO2 matrix by fission product (rare earth) doping.31-32

Figure 12 shows that the demand for H2 from steel corrosion ([H2]crit) decreases substantially as the decomposition ratio (the fraction of H2O2 decomposed, as opposed to causing corrosion) increases, but increases as the fracture depth increases. As O2, an alternative oxidant for UO2, is produced by decomposition, the influence of this reaction remains to be fully investigated.

**4.4 | Model Validation**

An attempt to validate the model has been made by comparing model predictions to a wide range of corrosion rate measurements as a function of α-source strength. Figure 13. These measurements were conducted on a wide range of specimens (α-doped UO2, Pu-doped UO2, spent fuels, simulated spent fuels, and UO3) under different exposure conditions. Despite the variability in the values, a clear trend of increasing corrosion rate with increasing α-source strength was established. In Figure 13, three sets of data (marked A, B, and C) cannot be considered to fit the linear relationship. For A, corrosion rates were calculated based on electrochemical impedance spectroscopy measurements, in which large errors due to the high resistance of the materials led to the overestimation of the rates. The value labeled B was measured in a clay environment containing reducing species, leading to unexpectedly low values. The values labeled C were measured on Pu-containing specimens, and it has been suggested that the low rates indicate a stabilizing influence of Pu on the UO2 matrix.

To appropriately test the model, only measurements performed on α-doped UO2 (with 233U and 238Pu) were used. As the measurements were normally performed in an oxygen-free environment in an open system, this would allow gases generated directly or indirectly by α-radiolysis, such as O2 and H2, to escape. To account for this, the boundary condition for H2 and O2 at the diffusion boundary was set with concentrations equal to zero. In addition, reactions involving e-particles and reactions involving scavengers produced by steel corrosion were also removed.34

Figure 14 compares the model prediction to the experimental values and demonstrates a very good correlation. This agreement, and a series of sensitivity calculations for various model parameters, demonstrate that the dominant factor controlling the corrosion rate is the rate of radiolytic production of...
H₂O₂, which is directly proportional to the α-source strength of the fuel, a feature determined by the extent of in-reactor burn-up.

**References**